



Non-spherical particle mixing behaviors by spherical inert particles assisted in a fluidized bed

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Received: 26 August 2019
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Abstract

Fluidized beds are widely used in many industrial fields such as petroleum, chemical and energy. In actual industrial processes, spherical inert particles are typically added to the fluidized bed to promote fluidization of non-spherical particles. Understanding mixing behaviors of binary mixtures in a fluidized bed has specific significance for the design and optimization of related industrial processes. In this study, the computational fluid dynamic–discrete element method with the consideration of rolling friction was applied to evaluate the mixing behaviors of binary mixtures comprising spherocylindrical particles and spherical particles in a fluidized bed. The simulation results indicate that the differences between rotational particle velocities were higher than those of translational particle velocities for spherical and non-spherical particles when well mixed. Moreover, as the volume fraction of the spherocylindrical particles increases, translational and rotational granular temperatures gradually increase. In addition, the addition of the spherical particles makes the spherocylindrical particles preferably distributed in a vertical orientation.

Keywords Non-spherical particle · Fluidized bed · Discrete element method · Binary mixtures

Abbreviations

CFD Computational fluid dynamic
DEM Discrete element method
LSD Linear spring dashpot

List of symbols

C_D Drag coefficient
 d_p Particle diameter, m
 F_c Contact force, N
 F_d Drag force, N
 g Gravitational acceleration, m/s^2
 I_p Moment of inertia, $kg\ m^2$
 k Spring stiffness, N/m
 m_p Particle mass, kg

M_{Lacey} Lacey mixing index
 N Number
 Re Reynolds number
 r_p Position of particle center, m
 S_p Momentum exchange source term, $kg/(m^2\ s^2)$
 t Time, s
 T_c Torque generated by contact force, N m
 T_r Torque generated by rolling friction, N m
 u_g Gas velocity, m/s
Vol Volume fraction of spherocylindrical particles
 V_p Particle volume, m^3
 v_p Particle translational velocity, m/s

Subscript

c Contact
g Gas phase
L Local coordinate system
n Normal direction
p Particle phase
rot Rotation
t Tangential direction
tran Translation

Greek letters

β Interphase momentum exchange coefficient, $kg/(m^3\ s)$
 δ Elastic deformation, m

Handling Editor: Jun Yao

Edited by Xiu-Qiu Peng

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ε	Volume fraction
$\theta_{p,tran}$	Translational granular temperature, $m^2 s^{-2}$
$\theta_{p,rot}$	Rotational granular temperature, $rad^2 s^{-2}$
μ	Friction coefficient
μ_g	Gas shear viscosity, Pa s
ρ	Density, kg/m^3
τ	Stress tensor
ω	Rotational velocity, rad/s
χ	Voidage function exponent
σ	Variance
Φ	Sphericity
Φ_{\perp}	Crosswise sphericity
Φ_{\parallel}	Lengthwise sphericity

1 Introduction

Fluidized beds are widely used in many industrial fields such as petroleum, chemical and energy due to their uniform mixing, large contact surfaces between phases and efficient heat transfer and mass transfer (Van Der Hoef et al. 2006). Many studies and applications have shown that circulating fluidized beds have become an important reactor for the combustion and utilization of petroleum coke (Chen and Lu 2007). The process of biomass conversion and utilization is also often carried out in a fluidized bed (Cui and Grace 2007). However, fluidization of biomass particles is a difficult task because the non-spherical biomass particles are generally large and have a low density. In the actual industrial processes, inert particles such as silica sand, alumina and calcite are often added to the biomass to assist its fluidization (Fotovat et al. 2013). Therefore, understanding mixing behaviors of binary mixtures in a fluidized bed has specific significance for the design and optimization of related industrial processes.

In recent years, many researchers have conducted experimental studies on the macroscopic flow and mixing behaviors of granular systems containing non-spherical particles. Zhang et al. (2009) experimentally studied the mixing and separation behaviors of biomass–sand binary mixture in a fluidized bed and analyzed the variation of flow pattern and mixing index. Fotovat et al. (2014) investigated effects of superficial gas velocity and the mixture composition on the mixing/segregation characteristics by analyzing the circulatory motion of the active tracer. Shao et al. (2016) investigated the mixing behaviors in binary-component and multi-component particulate systems and found that the density of non-spherical particles has a more significant influence on the mixing characteristics than particle size and shape. Boer et al. (2018) developed a digital image analysis technique to explore the particle distributions in the fluidized

bed and obtained qualitative and quantitative experimental results which can be used for validation of numerical models concerning non-spherical particle mixing. In general, it is difficult to obtain microscopic flow characteristics through experimental methods, and numerical simulation can obtain more detailed information, which is a good complement to the experiment. Among the many simulation methods, the computational fluid dynamics–discrete element method (CFD–DEM) has attracted much attention due to the fact that the motion characteristics of each particle can be obtained. Tsuji et al. (1993) coupled DEM proposed by Cundall and Strack (1979) with CFD to describe the gas–solid two-phase flow in fluidized beds. Currently, CFD–DEM has been widely used to evaluate the flow characteristics of spherical particles in bubbling fluidized beds (Müller et al. 2008; Luo et al. 2014; Wang et al. 2015; Wang et al. 2016a, b; Liu and van Wachem 2019), spouted beds (Takeuchi et al. 2004; He et al. 2016) and spouted fluidized beds (Luo et al. 2015; Van Buijtenen et al. 2011; Tang et al. 2017; Wang et al. 2016c).

In previous studies, the assumption of spherical particles was common. However, in the actual industrial process, particles are mostly non-spherical particles, and particle shape has a great influence on the macroscopic flow characteristics (Hilton et al. 2010). Recently, some scholars have applied CFD–DEM to study non-spherical particle flow behaviors in a fluidized bed. Hilton et al. (2010) studied the flow characteristics of spherical particles, cubes and ellipsoidal particles in a fluidized bed and found that the non-spherical particles have larger drag force at the same superficial gas velocity, leading to earlier fluidization. Zhou et al. (2011) evaluated the flow characteristics of ellipsoidal particles and analyzed the effect of aspect ratio on particle orientation and force structure. Cai et al. (2012) investigated the orientation distribution of cylindrical particles in the riser and found that the orientation of cylindrical particles is affected by their position more than the shape and local gas velocity.

In the process of fluidization and utilization of biomass, mixtures comprising non-spherical particles are often involved. Therefore, it is necessary not only to study the flow characteristics of the monocomponent non-spherical particle system, but also to further investigate the mixing characteristics of the multi-component non-spherical particle system. Ren et al. (2013) investigated the mixing behavior of binary mixtures comprising corn-shaped particles and spheres in a spouted bed and pointed out that particles with closer sizes could be better mixed. Vollmari et al. (2015) evaluated the mixing behavior bidisperse mixtures of various shaped particles and found that the mixing was strongly influenced by the shape of the particles and the addition of plates can accelerate the mixing. Ma and Zhao (2018) investigated the fluidization of binary mixtures comprising spheres and

rod-like particles and analyzed the effect of volume fraction of the rod-like particles on the minimum fluidization velocity and particle orientation.

Currently, there are few simulation studies on the mixing characteristics of binary mixtures containing non-spherical particles in a fluidized bed, and the understanding of microscopic characteristics such as granular temperature and particle orientation in the bed is not sufficient. Therefore, it is necessary to further investigate the mixing behavior and microscopic characteristics of binary mixtures containing non-spherical particles in a fluidized bed. In this study, CFD–DEM simulations with rolling resistance were carried out to evaluate the mixing behaviors of binary mixtures comprising spherocylindrical particles and spherical particles in a fluidized bed. The macroscale mixing behaviors and microscale hydrodynamic characteristics including granular temperature and particle orientation were discussed.

2 Model description

2.1 Gas phase

The gas phase is considered to be a continuous phase and modeled by the volume-averaged Navier–Stokes equations as shown below:

$$\frac{\partial(\epsilon_g \rho_g)}{\partial t} + \nabla \cdot (\epsilon_g \rho_g \mathbf{u}_g) = 0 \tag{1}$$

$$\frac{\partial(\epsilon_g \rho_g \mathbf{u}_g)}{\partial t} + \nabla \cdot (\epsilon_g \rho_g \mathbf{u}_g \mathbf{u}_g) = -\epsilon_g \nabla P - \mathbf{S}_p - \nabla \cdot (\epsilon_g \boldsymbol{\tau}_g) + \epsilon_g \rho_g \mathbf{g} \tag{2}$$

where ϵ_g is the porosity; t is the time, s; \mathbf{u}_g is the velocity of gas phase, m/s; ρ_g is the density of gas phase, kg/m³; \mathbf{S}_p is the momentum exchange source term, kg/(m² s²); $\boldsymbol{\tau}_g$ is the viscous stress tensor, kg/(m s²).

$$\mathbf{S}_p = -\frac{1}{V_c} \sum_i^{N_c} \mathbf{F}_{di} \tag{3}$$

$$\boldsymbol{\tau}_g = \frac{2}{3} \mu_g (\nabla \cdot \mathbf{u}_g) \mathbf{I} - \mu_g \left[(\nabla \mathbf{u}_g) + (\nabla \mathbf{u}_g)^T \right] \tag{4}$$

where V_c is the characteristic fluid volume, m³; N_c is the number of particles in the characteristic fluid volume; \mathbf{F}_d is the drag force, N; μ_g is the gas shear viscosity, Pa s; \mathbf{I} is the unit tensor.

2.2 Solid phase

The solid phase is treated to be a discrete phase, and the motion of each individual particle is directly solved by Newton’s second law. The translational motion equation of a non-spherical particle is given as follows:

$$m_p \frac{d^2 \mathbf{r}}{dt^2} = -V_p \nabla P + m_p \mathbf{g} + \mathbf{F}_c + \mathbf{F}_d \tag{5}$$

where m_p is the mass of particle, kg; \mathbf{r} is the position of particle center, m; \mathbf{v}_p is the translational velocity of particle, m/s; \mathbf{F}_c is the contact force, N.

In this study, each non-spherical particle is modeled by the multi-sphere method (Favier et al. 1999). In the multi-sphere method, the contact force and torque acting on a non-spherical particle are obtained by calculating the sum of

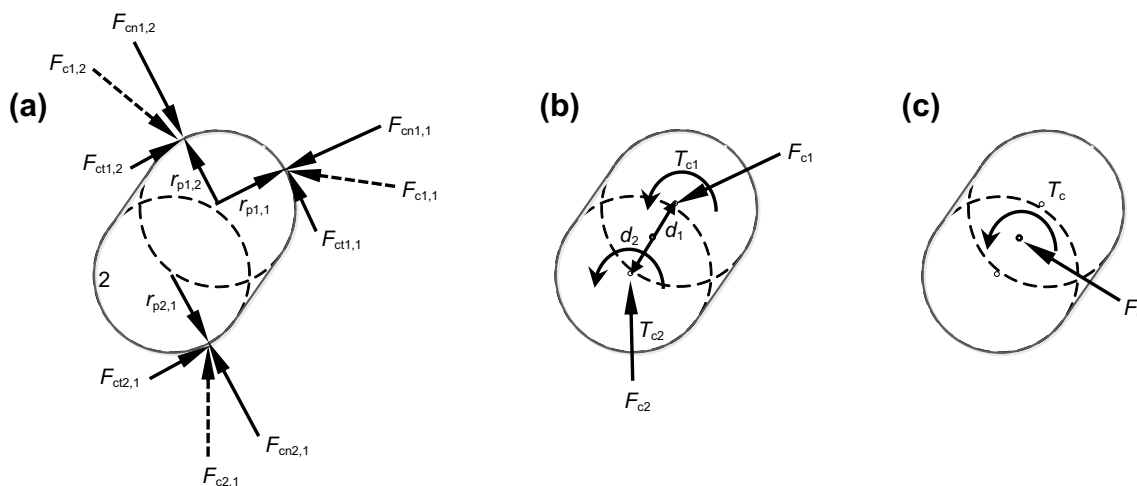


Fig. 1 Schematic diagram of transferring the force acting on the elemental sphere to the centroid of a non-spherical particle. **a** Forces, respectively, acting on each element sphere; **b** forces and torques acting on the center of each element sphere; **c** forces and torques acting on the center of a non-spherical particle

contact forces and torques on its spherical elements. Figure 1 shows the schematic diagram of transferring the force acting on the elemental sphere to the centroid of a non-spherical particle. To reduce the computational cost, a two-step method (Wang et al. 2016b) was used for contact detection.

The contact force acting on spherical element was calculated using a linear spring-dashpot (LSD) model and consists of a normal component F_n and a tangential component F_t :

$$F_n = -k_n \delta_n - \eta_n v_n \tag{6}$$

$$F_t = \begin{cases} -k_t \delta_t - \eta_t v_t & |F_t| \leq \mu_f |F_n| \\ -\mu_f |F_n| \frac{v_t}{|v_t|} & |F_t| > \mu_f |F_n| \end{cases} \tag{7}$$

where k is the spring stiffness (N/m); δ is the elastic deformation (m); η is the damping coefficient (N s /m); v is the relative velocity (m/s); μ_f is the sliding friction coefficient. The subscripts n and t indicate the variables in normal direction and tangential direction, respectively.

Since the non-spherical particles inertia moment changes constantly during the rotation, the rotational motion of the non-spherical particles is more complicated than that of the spherical particles. To describe the rotational motion of non-spherical particles more conveniently, two coordinate systems are generally introduced: (a) a global coordinate system and (b) a local coordinate system. The angular momentum equation is solved in a local coordinate system, and the rotational variables are transformed between the local coordinate system and global coordinate system using the quaternion method (Wachem et al. 2015). As shown in

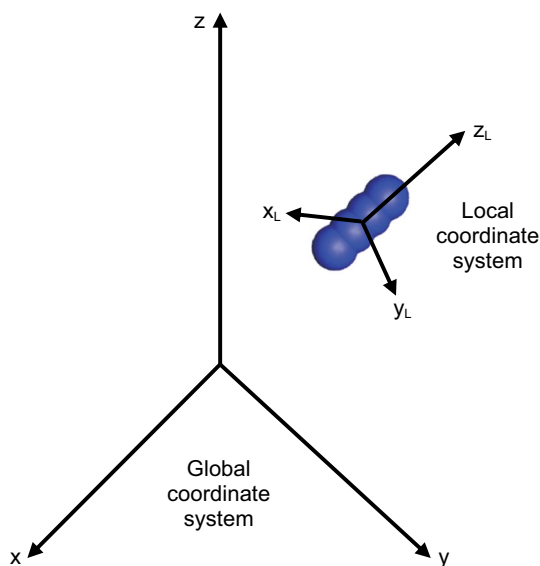


Fig. 2 Schematic diagram of the local coordinate system

Fig. 2, the direction of the coordinate axis of the local coordinate system is the direction of the principal axis of the particle's inertia.

$$I_L \frac{d\omega_L}{dt} + \omega_L \times (I_L \cdot \omega_L) = T_L = T_c + T_r \tag{8}$$

where I_L is the inertia tensor (kg m²); ω_L is the rotational velocity of particle in a local coordinate system (rad/s); T_L is the torque in a local coordinate system (N m); T_c is the torque generated by contact force (N m); T_r is the torque generated by rolling friction (N m).

The torque generated by rolling friction is attributed to the elastic hysteresis loss or viscous dissipation and slows down the relative rotations of particles (Zhou et al. 1999). Goniva et al. (2012) found that rolling friction can affect the velocity of spherical particles in spouted fluidized beds and simulation results can be improved significantly when applying a rolling friction model. In this study, the correlation proposed by Brilliantov and Pöschel (1998) was used to calculate the torque on contacting spherical elements generated by rolling friction as follows:

$$T_{ri} = -\mu r_p |F_n| \hat{\omega}_i \tag{9}$$

where μ is the rolling friction coefficient; r_p is the radius of spherical element (m); $|F_n|$ is the magnitude of normal contact force (N); ω is the rotational velocity of particle (rad/s).

2.3 Interphase exchange

Based on the drag force applied on a spherical particle, Di Felice (1994) proposed a drag correlation in multi-particle systems by experimental fitting.

$$F_d = \frac{1}{2} \rho_g C_D A_{\perp} |u_g - v_p| (u_g - v_p) \epsilon_g^{2-\chi} \tag{10}$$

$$\chi = 3.7 - 0.65 \exp \left[-\frac{(1.5 - \log_{10} Re)^2}{2} \right] \tag{11}$$

Based on the experimental data obtained from Leith (1987), Ganser (1993), Tran-Cong et al. (2004) and a comprehensive numerical study, Hölzer and Sommerfeld (2008) established a simple and accurate drag model for non-spherical particles:

$$C_D = \frac{8}{Re} \frac{1}{\sqrt{\Phi_{\parallel}}} + \frac{16}{Re} \frac{1}{\sqrt{\Phi}} + \frac{3}{\sqrt{Re}} \frac{1}{\Phi^{\frac{3}{4}}} + 0.42 \times 10^{0.4(-\log \Phi)^{0.2}} \frac{1}{\Phi_{\perp}} \tag{12}$$

where Φ is the sphericity, Φ_{\perp} is the crosswise sphericity, and Φ_{\parallel} is the lengthwise sphericity. Re is defined as follows,

$$Re = \frac{\epsilon_g d_p |\mathbf{u}_g - \mathbf{v}_p| \rho_g}{\mu_g} \quad (13)$$

In this study, Di Felice (1994) correlation and Hölzer and Sommerfeld (2008) drag model were used to describe inter-phase momentum exchange. This method has been used in many studies in non-spherical granular systems (Hilton et al. 2010; Gan et al. 2017; Ma et al. 2017).

2.4 Particle granular temperature

The particle granular temperature is the turbulent energy of particles, indicating the velocity fluctuations of particles (Tartan and Gidaspow 2004; Jung et al. 2005). The particle translational granular temperature is defined as the mean of second moment of particle translational velocity fluctuation:

$$\langle C_i C_j \rangle = \frac{1}{n} \sum_{k=1}^n [v_{p,ik}(x, t) - c_i(x, t)] [v_{p,jk}(x, t) - c_j(x, t)] \quad (14)$$

where i, j represent x, y or z directions, n is the number of particles in a unit volume, and $v_p(x, t)$ is the instantaneous translational velocity of particles. The average translational velocity $c_i(x, t)$ can be expressed as follows:

$$c_i(x, t) = \frac{1}{n} \sum_{k=1}^n v_{p,ik}(x, t) \quad (15)$$

Similarly, the particle rotational granular temperature ($\theta_{p,rot}(x, t)$) can be obtained as follows:

$$\langle C_{rot,i} C_{rot,j} \rangle = \frac{1}{n} \sum_{k=1}^n [\omega_{p,ik}(x, t) - c_{rot,i}(x, t)] [\omega_{p,jk}(x, t) - c_{rot,j}(x, t)] \quad (16)$$

where $\omega_p(x, t)$ is the instantaneous rotational velocity of particles. The average rotational velocity $c_{rot,i}(x, t)$ can be expressed as follows:

$$c_{rot,i}(x, t) = \frac{1}{n} \sum_{k=1}^n \omega_{p,ik}(x, t). \quad (17)$$

2.5 Initial and boundary conditions

As shown in Fig. 3, the dimension of the fluidized bed in the simulation was 150 mm, 20 mm and 400 mm in width, depth and height, respectively. At the bottom of fluidized bed, uniform airflow was injected through the air distribution plate. A pressure outlet boundary condition was used

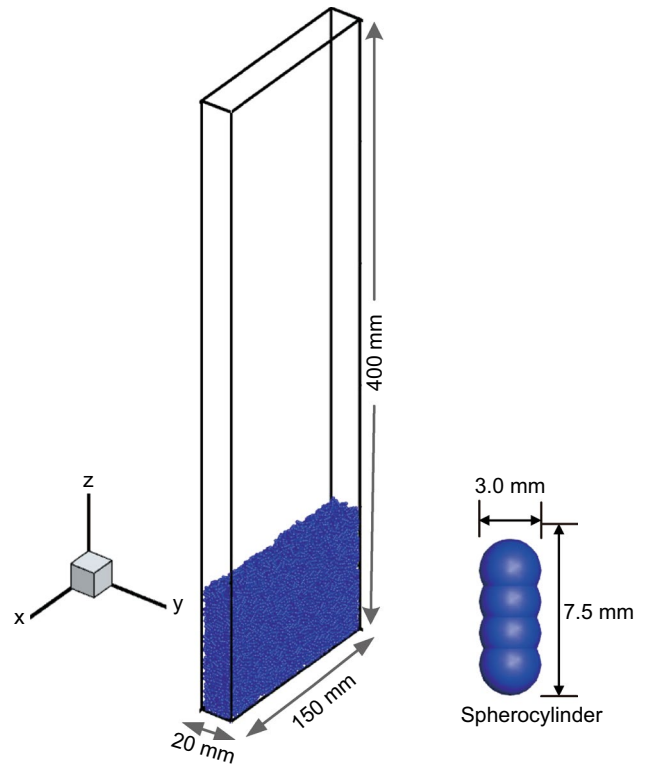


Fig. 3 Schematic geometry of the fluidized bed and the spherocylindrical particle

Table 1 Parameters applied in the simulation

Variable	Value	Unit
<i>Bed</i>		
Dimensions in x, y and z directions	150×20×400	mm
Grids in x, y and z directions	15×2×40	–
<i>Particles</i>		
Density, ρ_p	1050	kg/m ³
Coefficient of restitution, e	0.5	–
Coefficient of sliding friction between particles, μ_{f_pp}	0.4	–
Coefficient of rolling friction, μ	0.1	–
Coefficient of sliding friction between particle and wall, μ_{f_pw}	0.3	–
Normal spring stiffness, k_n	10,000	N/m
Tangential spring stiffness, k_t	3063.8	N/m
<i>Gas</i>		
Superficial gas velocity, U_g	1.6/2.0	m/s
Density, ρ_g	1.2	kg/m ³
Viscosity, μ_g	1.8×10 ⁻⁵	Pa s
Outlet pressure, P	101,325	Pa

at the top of the bed, and a no-slip boundary condition was applied at the walls for the gas phase. The spring stiffness and damping coefficient significantly affect the maximum overlap of particle collisions. Kruggel-Emden et al. (2010) suggested a maximum overlap of 1% of the particle diameter to avoid alteration of the simulations. The spring stiffness was chosen so that the maximum overlap condition is fulfilled. The parameters applied in the simulation are summarized in Table 1.

The particles in the simulation included spherical particles (3 mm in diameter) and spherocylindrical particles modeled by a multi-sphere method (7.5 mm in long diameter, 3 mm in short diameter, as shown in Fig. 3). The volume fraction of the spherocylinders (Vol) in the binary mixtures

in the fluidized bed was 100%, 75%, 50% and 25%, respectively. Composition of the granular systems in the simulation is summarized in Table 2. As shown in Fig. 4, at the initial moment ($t = 0$ s), the spherocylinders marked in blue are stacked above the spherical particles marked in red. In this study, the CFD time step is 5×10^{-5} s and the DEM time step is 5×10^{-6} s.

3 Results and discussion

3.1 Mixing behaviors

Figure 5 shows the instantaneous particle distribution at $t = 10$ s at $U_g = 1.6$ m/s and $U_g = 2.0$ m/s. It can be seen that under two superficial gas velocities, the spherocylindrical particles and the spherical particles are uniformly mixed at $t = 10$ s. In addition, due to the presence of the spherocylindrical particles, the large bubbles are not always in the middle of the bed and may appear in the vicinity of the left and right walls. It can also be observed that the bed expansion height is higher with superficial gas velocity of 2.0 m/s.

The averaged translational velocities of the spherocylindrical particles and spherical particles during 0–10 s are

Table 2 Composition of the granular systems in the simulation

The volume fraction of the spherocylinders (Vol), %	Number of the spherocylinders	Number of the spheres
100	4000	0
75	3000	3240
50	2000	6480
25	1000	9720

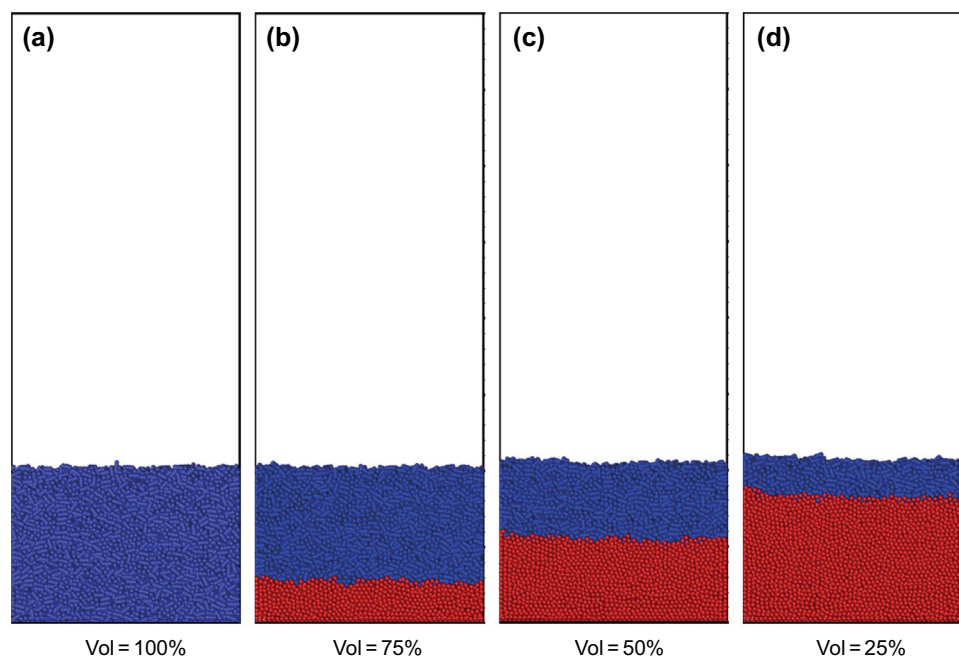


Fig. 4 Initial particle distribution in the fluidized bed (spherocylindrical particles marked in blue; spherical particles marked in red). **a** Vol = 100%, **b** Vol = 75%, **c** Vol = 50%, **d** Vol = 25%

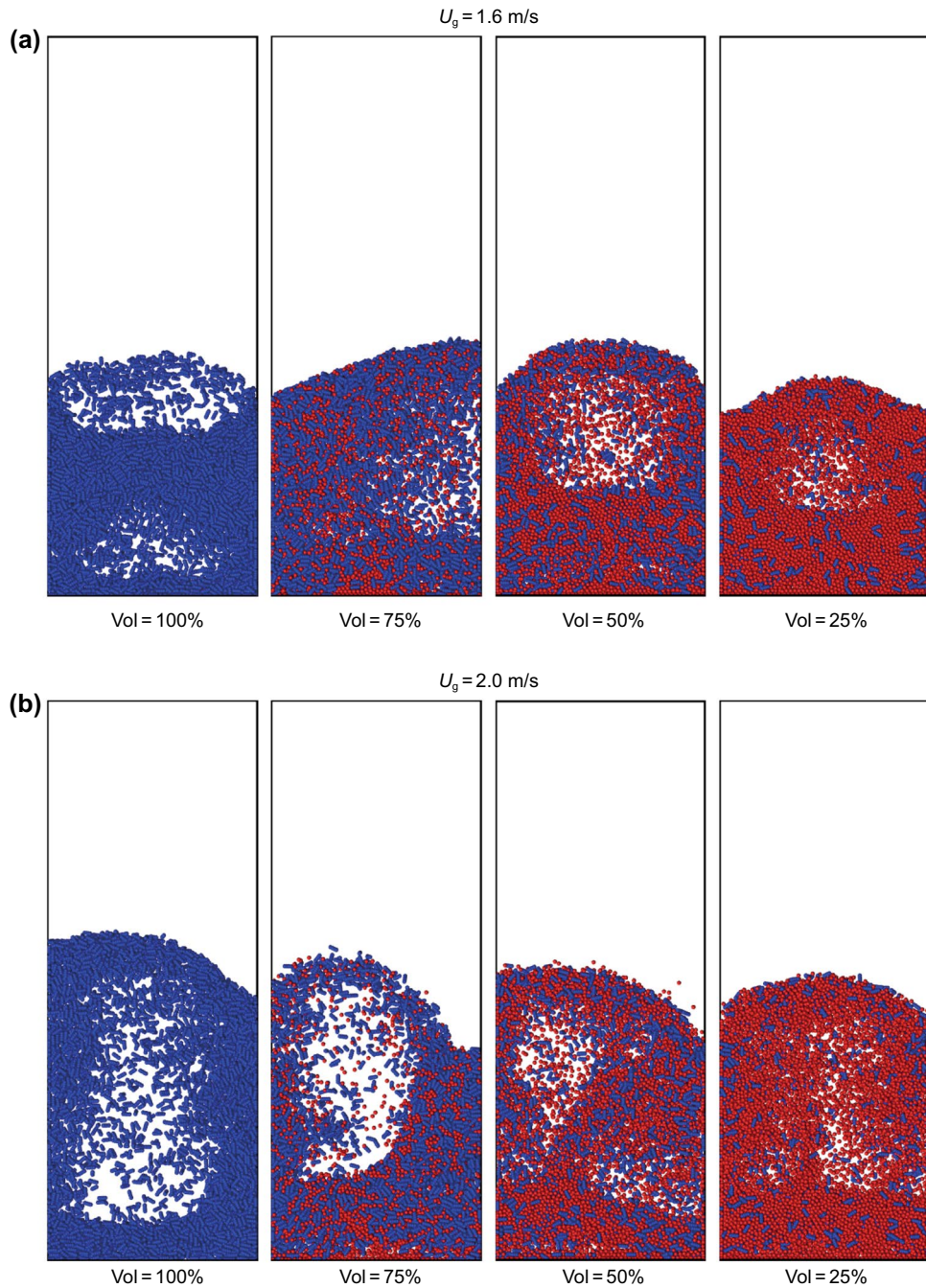


Fig. 5 Snapshots of particle distribution at $t=10$ s at $U_g=1.6$ m/s and $U_g=2.0$ m/s, **a** $U_g=1.6$ m/s (Vol=100%, Vol=75%, Vol=50%, Vol=25%), **b** $U_g=2.0$ m/s (Vol=100%, Vol=75%, Vol=50%, Vol=25%)

shown in Fig. 6. The average particle translational velocities are calculated as follows:

$$|v_p| = \frac{1}{N} \sum_{i=1}^N \sqrt{v_{px}^2 + v_{py}^2 + v_{pz}^2} \quad (18)$$

It can be found that the instantaneous average translational velocities of the spherocylindrical particles at the initial stage are greater than that of the spherical particles, but after a few seconds, the average translational velocities

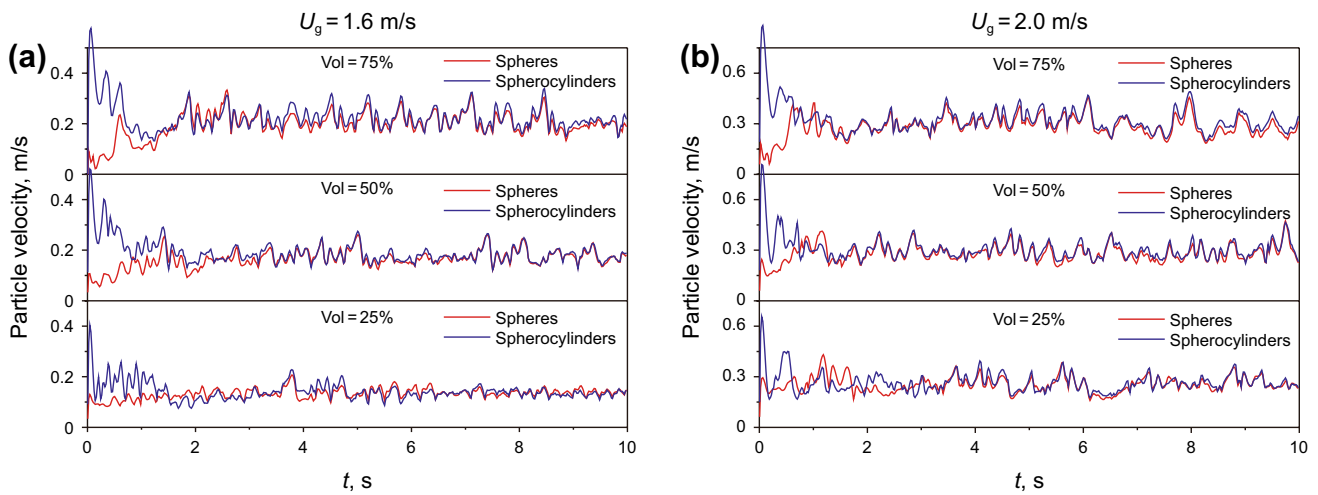


Fig. 6 The average translational velocities of the spherocylindrical particles and spherical particles during 0–10 s at **a** $U_g=1.6$ m/s and **b** $U_g=2.0$ m/s

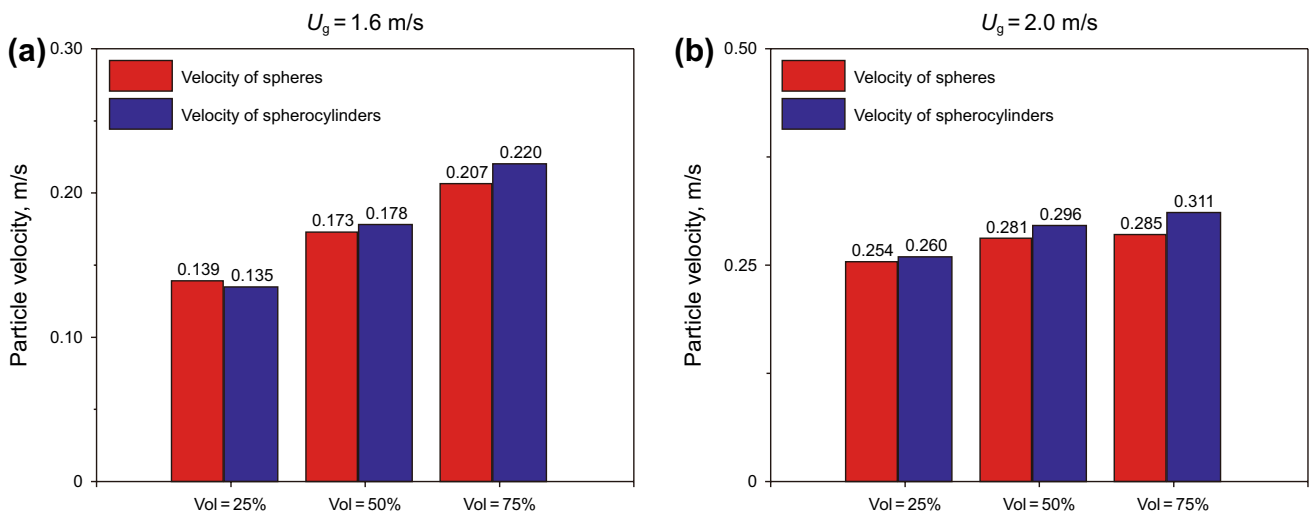


Fig. 7 Time-averaged translational velocities of the spherocylindrical particles and spherical particles during 5–10 s at **a** $U_g=1.6$ m/s and **b** $U_g=2.0$ m/s

of the two particles become very close. The time required for particle mixing can be roughly estimated by the moment when the average velocities of the two particles become very close. Particles mix faster when the superficial gas velocity is 2.0 m/s, compared with the superficial gas velocity of 1.6 m/s.

Moreover, Fig. 7 shows time-averaged translational velocities of the spherocylindrical particles and spherical

particles during 5–10 s. It can be clearly seen that as the superficial gas velocity increases, time-averaged translational particle velocities in the bed increase. In addition, as the volume fraction of the spherocylindrical particles increases, time-averaged translational particle velocities in the bed also increase. This might be explained that non-spherical particles have larger drag at the same superficial gas velocity.

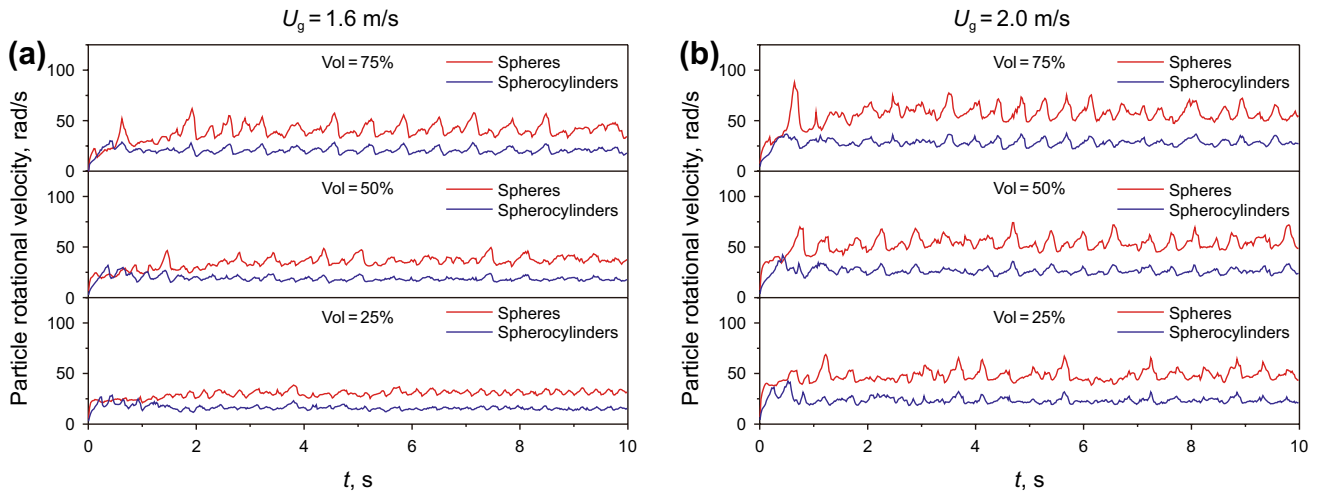


Fig. 8 The average rotational velocities of the spherocylindrical particles and spherical particles. **a** $U_g = 1.6$ m/s, **b** $U_g = 2.0$ m/s

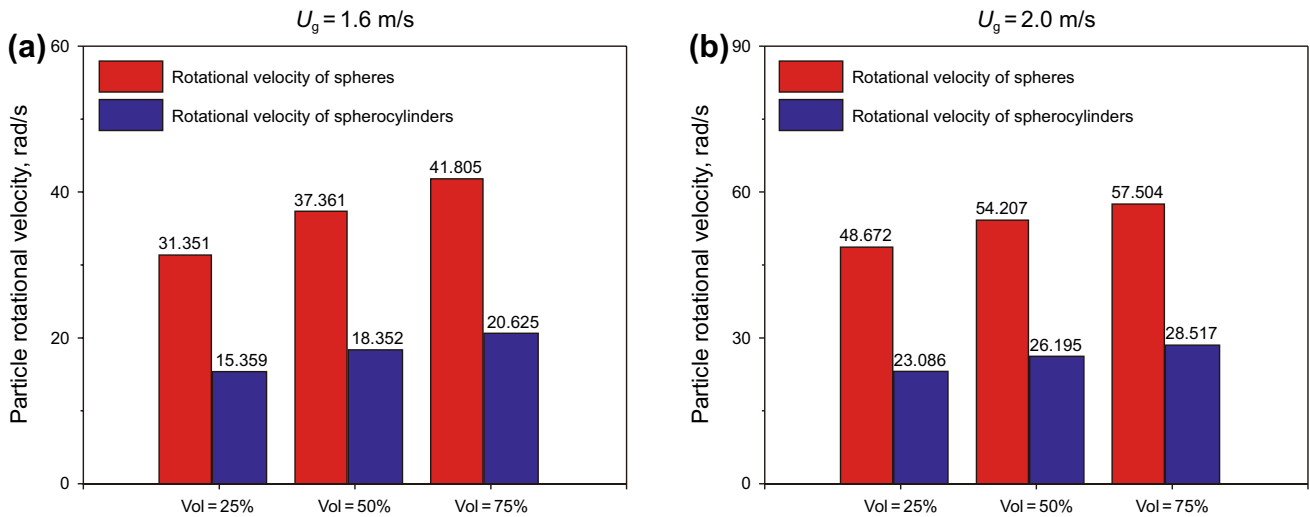


Fig. 9 Time-averaged rotational velocities of the spherocylindrical particles and spherical particles during 5–10 s at **a** $U_g = 1.6$ m/s and **b** $U_g = 2.0$ m/s

The averaged rotational velocities of the spherocylindrical particles and spherical particles during 0–10 s are shown in Fig. 8. The average particle rotational velocities are calculated by:

$$|\omega_p| = \frac{1}{N} \sum_{i=1}^N \sqrt{\omega_{px}^2 + \omega_{py}^2 + \omega_{pz}^2} \quad (19)$$

It can be observed that even if the particles are uniformly mixed, the average rotational velocities of the spherical particles are larger than that of the spherocylindrical particles. This may be due to the fact that the spherocylindrical particles are in contact with more particles and the rotational resistance is larger.

In addition, Fig. 9 shows time-averaged rotational velocities of the spherocylindrical particles and spherical particles during

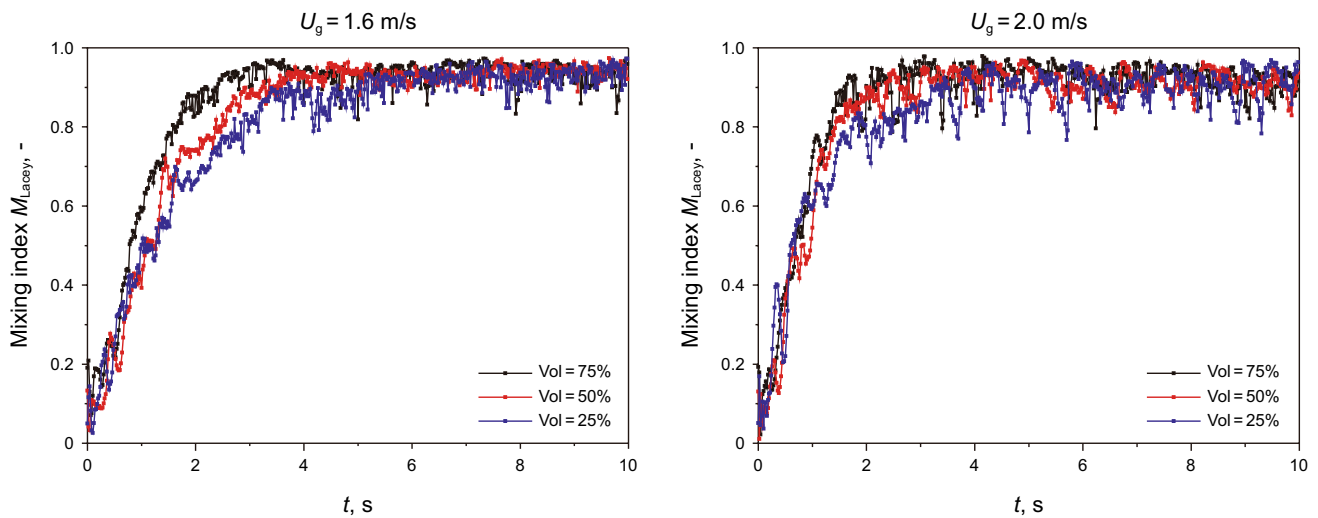


Fig. 10 Variation of Lacey mixing index with time at $U_g = 1.6 \text{ m/s}$ and $U_g = 2.0 \text{ m/s}$

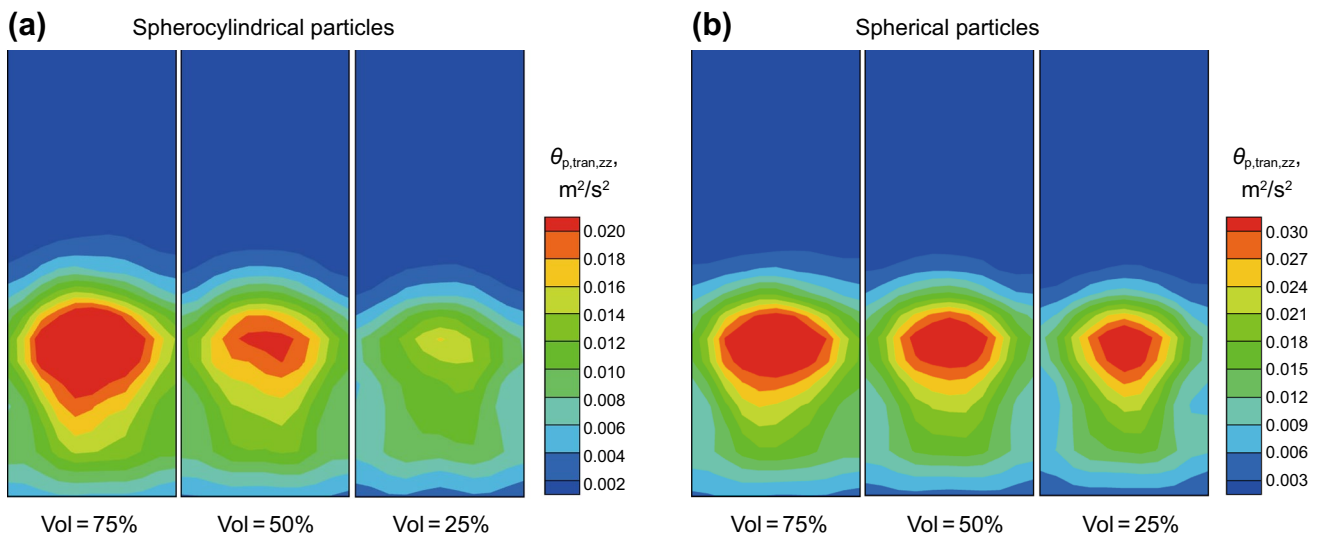


Fig. 11 Translational granular temperature distribution in z direction ($U_g = 2.0 \text{ m/s}$). **a** Spherocylindrical particles (Vol = 75%, Vol = 50%, Vol = 25%), **b** spherical particles (Vol = 75%, Vol = 50%, Vol = 25%)

5–10 s. The results indicate that time-averaged rotational particle velocities in the bed increase with the increase in superficial gas velocity. As the volume fraction of the spherocylindrical particles increases, time-averaged rotational particle velocities in the bed also increase slightly.

To further analyze the particle mixing process, the Lacey mixing index (Lacey 1954) was used to quantitatively describe the mixing of binary particles:

$$M_{Lacey} = \frac{\sigma_0^2 - \sigma_r^2}{\sigma_0^2 - \sigma_r^2} \tag{20}$$

The variance defined as the square of the standard deviation can be calculated by the following formula:

$$\sigma^2 = \frac{1}{N-1} \sum_{i=1}^N (c_i - \bar{c})^2 \tag{21}$$

where N is the number of subcells; c_i is the local concentration of sample particles; \bar{c} is the average concentration of sample particles; and σ_0^2 and σ_r^2 are the variances of the fully separated state and the completely mixed state, respectively.

The Lacey mixing index is 0 for the fully separated state, and the Lacey mixing index is 1 for the completely mixed state. The spherocylindrical particles are equally divided into equal volumes of spherical elements, and then, the Lacey mixing index is calculated using spherical elements and spherical particles. Figure 10 shows the Lacey mixing index during 0–10 s at the superficial gas velocity of 1.6 m/s and 2.0 m/s. It can be seen that the mixing index of both superficial gas velocities can reach a value close to 1, which indicates that the spherocylindrical particles and the spherical particles can achieve good mixing. However, corresponding mixing index can reach the stability more quickly when the superficial gas velocity is 2.0 m/s, which demonstrates that increasing the superficial gas velocity can accelerate the mixing of the particles. Moreover, when the superficial gas velocity is the same, as the volume fraction of the spherocylindrical particles increases, the particle mixing is slightly accelerated.

3.2 Particle granular temperature distribution

Figure 11 presents the time-averaged translational granular temperatures of spherocylindrical particles and spherical particles in z direction. The translational granular temperature is the translational turbulent energy of particles, indicating the translational velocity fluctuations of particles. It can be observed that the translational granular temperature of the spherical particles is slightly larger than that of the spherocylindrical particles. Moreover, as the volume fraction of the spherocylindrical particles increases, the translational granular temperature of the particles gradually increases, which means that the fluctuation of the translational velocity of the particles becomes more severe.

Similarly, the rotational granular temperature is the rotational turbulent energy of particles, indicating the rotational velocity fluctuations of particles. In a pseudo-2D fluidized bed, y direction is the primary direction for rotation of particles. Figure 12 shows the time-averaged rotational granular temperatures of spherocylindrical particles and spherical particles in y direction. It can be clearly seen that the rotational granular temperature of the spherical particles is much larger than that of the spherocylindrical particles. This indicates that the fluctuation of the rotational velocity of the spherical particles is much more severe than that of the spherocylindrical particles. In addition, as the volume

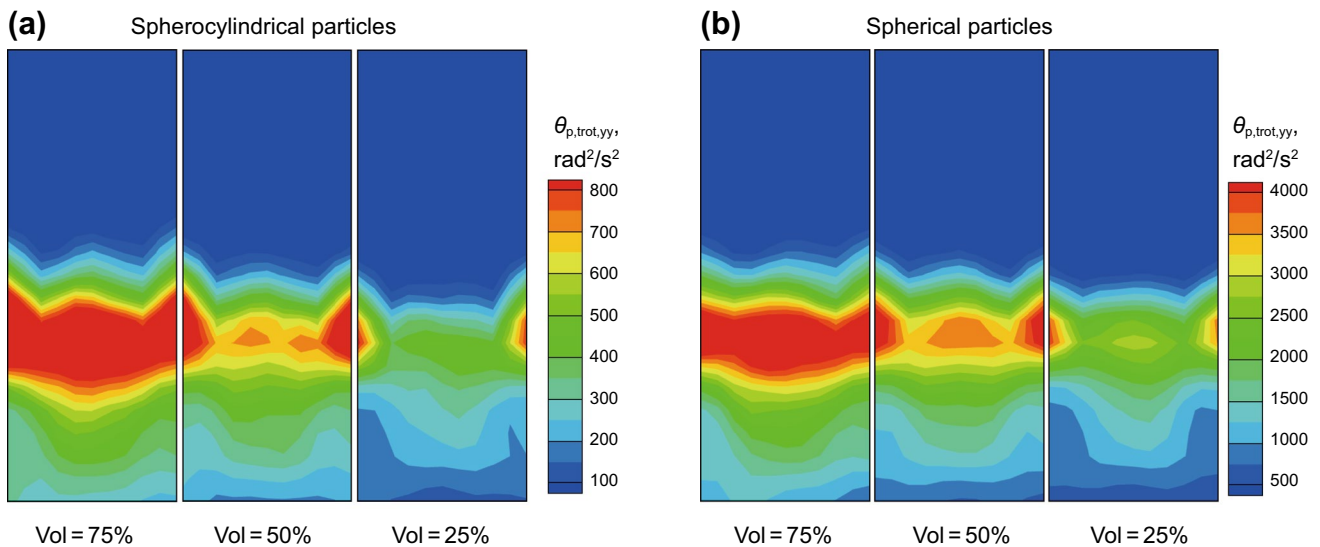


Fig. 12 Rotational granular temperature distribution in y direction ($U_g=2.0$ m/s), **a** spherocylindrical particles (Vol=75%, Vol=50%, Vol=25%), **b** spherical particles (Vol=75%, Vol=50%, Vol=25%)

fraction of the spherocylindrical particles increases, the rotational granular temperature of the particles gradually increases.

3.3 Particle orientation distribution

The orientation of the spherocylindrical particles significantly affects the fluidization and mixing of particles. In this paper, the orientation angle was defined on the $X-O-Z$ plane and varied from 0° to 90° for quantification, similar to the definition of Zhou et al. (2011). 0° corresponds to the particles in horizontal direction (the long axis of the particle is parallel to the x -axis), and 90° represents the particles in vertical direction (the long axis of the particle is parallel to the z -axis). A schematic view of the orientation angle of spherocylindrical particles is shown in Fig. 13a. The orientation angle is divided into six ranges with an interval of 15° (i.e., $0^\circ-15^\circ$, $15^\circ-30^\circ$, $30^\circ-45^\circ$, $45^\circ-60^\circ$, $60^\circ-75^\circ$, $75^\circ-90^\circ$), and particles are counted at every angle range to calculate the percentage distribution of particle orientation.

Figure 13 shows the percentage distribution of particle orientation for Vol = 100% during 0–10 s at the superficial gas velocity of 1.6 m/s and 2.0 m/s. It can be seen that the spherocylindrical particles tend to be horizontally oriented at the initial packing state. When entering the fluidization stage, the tendency of the horizontal orientation of the spherocylindrical particles is weakened, and the tendency of the vertical orientation is increased. Moreover, the results indicate that as the superficial gas velocity increases, the tendency of the horizontal orientation of the rod-shaped particles decreases, and the particles tend to be more vertically oriented.

Figure 14 shows the percentage distribution of the orientation of the spherocylindrical particles at the superficial gas velocity of 2.0 m/s. It can be found that as the volume fraction of the spherocylindrical particles decreases, the percentage of the vertical orientation increases, that is, the addition of the spherical particles makes the spherocylindrical particles preferably distributed in a vertical orientation. There are two possible reasons for the vertical orientation of the spherocylindrical particles in a fluidized bed. On the one hand, it is related to the action of the drag force. When the spherocylindrical particles are horizontally oriented, the cross-sectional area in the vertical flow direction is large, resulting in a large drag force, which causes the particles to move in a direction in which the flow resistance is reduced. On the other hand, the addition of spherical particles increases the voids in the fluidized bed. The increase in the movement space of the spherocylindrical particles helps to reduce the interlocking phenomenon and promote

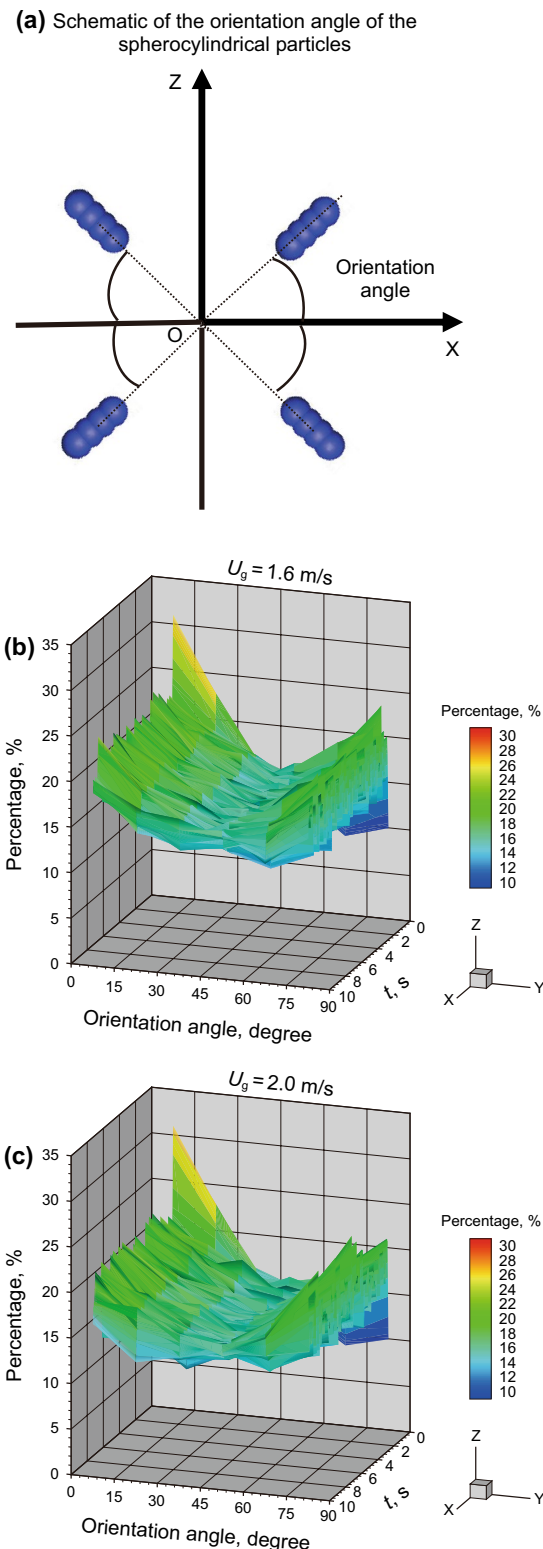


Fig. 13 Particle orientation distribution at $U_g = 1.6 \text{ m/s}$ and $U_g = 2.0 \text{ m/s}$ (Vol = 100%), a schematic of the orientation angle of the spherocylindrical particles, b $U_g = 1.6 \text{ m/s}$, c $U_g = 2.0 \text{ m/s}$

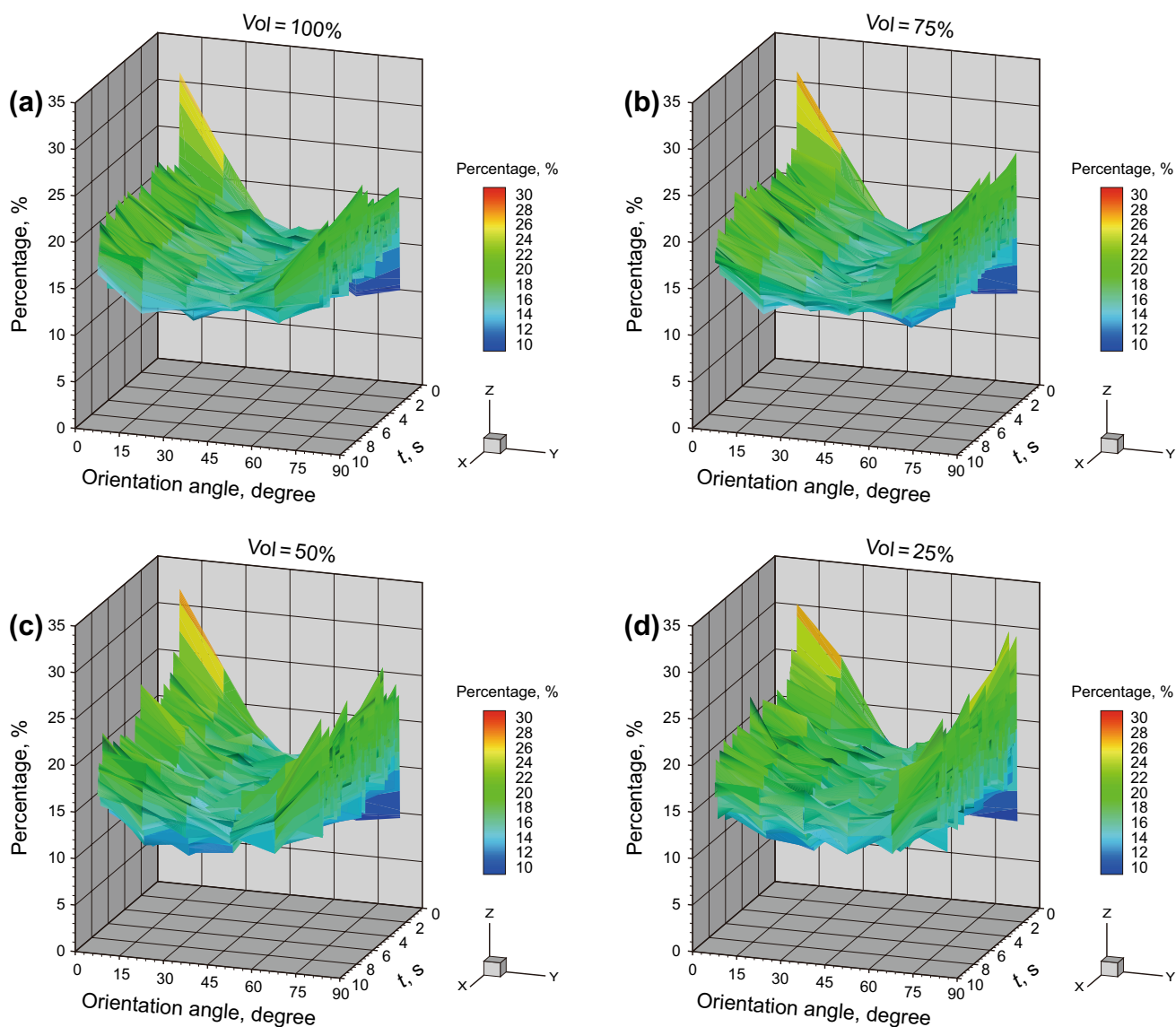


Fig. 14 Particle orientation distribution ($U_g = 2.0$ m/s), **a** Vol = 100%, **b** Vol = 75%, **c** Vol = 50%, **d** Vol = 25%

the fluidization of the spherocylindrical particles. In conclusion, the combined effect of the two aspects makes the spherocylindrical particles in the binary granular system preferably oriented vertically.

In order to investigate the orientation distribution of the binary mixture in the vicinity of the walls, the time-average orientation of the spherocylindrical particles in each 10-mm

region near the left- and right-side walls (marked in blue) is counted as shown in Fig. 15. It can be seen that the particles in the vicinity of the side walls are more vertically oriented due to the wall effect. The superficial gas velocity increases, and the vertical orientation trend is still obvious, indicating that the wall effect dominates the orientation behavior of the spherocylindrical particles in the vicinity of the walls.

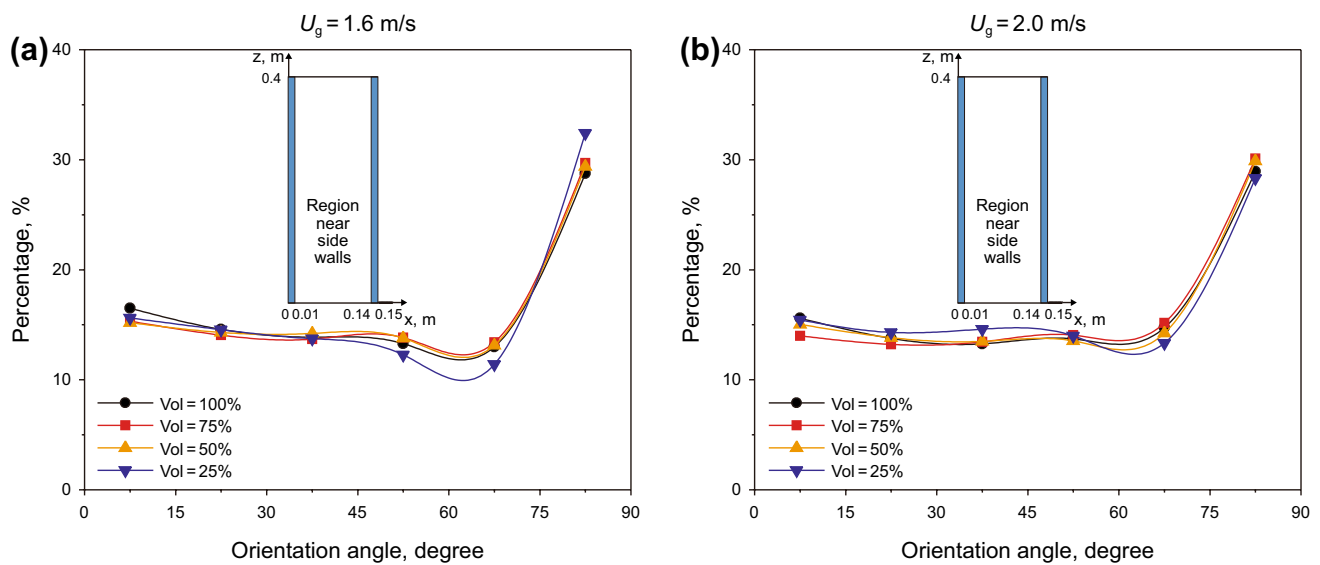


Fig. 15 Particle orientation distribution in the vicinity of the left and right walls, **a** $U_g = 1.6$ m/s, **b** $U_g = 2.0$ m/s

4 Conclusion

In this study, CFD–DEM approach with rolling resistance was applied to evaluate the mixing behaviors of binary mixtures comprising spherocylindrical particles and spherical particles in a fluidized bed. The effects of the volume fraction of the spherocylindrical particles on the macroscopic mixing characteristics and microscopic flow behaviors including granular temperature and orientation distribution were discussed.

Increasing the superficial gas velocity accelerates the mixing process of the particles. Furthermore, when the superficial gas velocity is the same, as the volume fraction of the spherocylindrical particles increases, the particle mixing is slightly accelerated. Moreover, when well mixed, the average translational velocities of the spherocylindrical and spherical particles become very close, but the average rotational velocities of the spherical particles are larger.

In the fluidized bed, the translational granular temperature of the spherical particles is slightly larger than that of the spherocylindrical particles and the rotational granular temperature of the spherical particles is much larger than that of the spherocylindrical particles. Moreover, as the volume fraction of the spherocylindrical particles increases, the translational and rotational granular temperatures of the particles gradually increase.

In the binary granular system, as the volume fraction of the spherocylindrical particles decreases, the percentage of the vertical orientation increases, that is, the addition of the spherical particles makes the spherocylindrical particles preferably distributed in a vertical orientation. In addition,

the wall effect dominates the orientation behavior of the spherocylindrical particles in the vicinity of the walls.

Acknowledgements This work is financially supported by the National Natural Science Foundation of China (Grant No. 51706055).

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